

## UNIT 3 • LINEAR AND EXPONENTIAL FUNCTIONS

### Lesson 7: Operating on Functions and Transformations

#### Instruction

#### Guided Practice 3.7.1

##### Example 1

If  $f(x) = 3x + 2$  and  $g(x) = 2x - 7$ , what is the result of adding the two functions? What is  $(f + g)(x)$ ? How do you represent this algebraically?

1. Add the two function rules.

$$(f + g)(x) = f(x) + g(x)$$

Since  $f(x) = 3x + 2$  and  $g(x) = 2x - 7$ ,  $(f + g)(x) = (3x + 2) + (2x - 7)$ .

2. Combine like terms.

Clear the parentheses and reorder the terms on the right side of the equation.

$$(f + g)(x) = (3x + 2) + (2x - 7) \quad \text{Equation}$$

$$(f + g)(x) = 3x + 2 + 2x - 7 \quad \text{Remove the parentheses.}$$

$$(f + g)(x) = 3x + 2x + 2 - 7 \quad \text{Reorder the terms: variables with coefficients first, followed by constants.}$$

3. Simplify the equation.

$$(f + g)(x) = 3x + 2x + 2 - 7 \quad \text{Equation}$$

$$(f + g)(x) = 5x - 5$$

The result of adding  $f(x) = 3x + 2$  and  $g(x) = 2x - 7$  is  $(f + g)(x) = 5x - 5$ .



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#### Example 2

If  $f(x) = 3^x$  and  $g(x) = 5$ , what is the result of multiplying the two functions? What is  $(f \cdot g)(x)$ ? How do you represent this algebraically?

1. Multiply the two function rules.

$$(f \cdot g)(x) = f(x) \cdot g(x)$$

$$\text{Since } f(x) = 3^x \text{ and } g(x) = 5, (f \cdot g)(x) = (3^x) \cdot (5).$$

2. Simplify the equation.

$$(f \cdot g)(x) = (3^x) \cdot (5) \quad \text{Equation}$$

$$(f \cdot g)(x) = 5(3^x)$$

$$(f \cdot g)(x) = 5(3^x) \text{ is the result of multiplying } f(x) = 3^x \text{ and } g(x) = 5.$$

#### Example 3

If  $f(x) = 2x - 3$  and  $g(x) = 4x - 11$ , what is the result of subtracting the two functions? What is  $(f - g)(x)$ ? How do you represent this algebraically?

1. Subtract the two function rules.

$$(f - g)(x) = f(x) - g(x)$$

$$\text{Since } f(x) = 2x - 3 \text{ and } g(x) = 4x - 11, (f - g)(x) = (2x - 3) - (4x - 11).$$

2. Combine like terms.

Clear the parentheses and reorder the terms on the right side of the equation. Be careful to correctly distribute the negative sign.

$$(f - g)(x) = (2x - 3) - (4x - 11) \quad \text{Equation}$$

$$(f - g)(x) = 2x - 3 - 4x + 11 \quad \text{Distribute the negative.}$$

$$(f - g)(x) = 2x - 4x - 3 + 11 \quad \text{Reorder the terms: variables with coefficients first, followed by constants.}$$

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3. Simplify the equation.

$$(f - g)(x) = 2x - 4x - 3 + 11 \quad \text{Equation}$$

$$(f - g)(x) = -2x + 8$$

$(f - g)(x) = -2x + 8$  is the result of subtracting  $f(x) = 2x - 3$  and  $g(x) = 4x - 11$ .



#### Example 4

If  $f(x) = 2^x$  and  $g(x) = 2$ , what is the result of dividing the two functions? What is  $(f \div g)(x)$ ? How do you represent this algebraically?

1. Divide the two function rules.

$$(f \div g)(x) = f(x) \div g(x)$$

Since  $f(x) = 2^x$  and  $g(x) = 2$ ,  $(f \div g)(x) = (2^x) \div 2$ .



2. Simplify the equation.

$$(f \div g)(x) = (2^x) \div 2 \quad \text{Equation}$$

$$(f \div g)(x) = \frac{2^x}{2} \quad \text{Simplify as needed.}$$

$$(f \div g)(x) = \frac{1}{2}(2^x)$$

$(f \div g)(x) = \frac{1}{2}(2^x)$  is the result of dividing  $f(x) = 2^x$  by  $g(x) = 2$ .

