Instruction

Guided Practice 1.3.1

Example 1

A local convenience store owner spent $10 on pencils to resell at the store. What is the equation of the store's revenue if each pencil sells for $0.50? Graph the equation.

1. Read the problem and then reread the problem, determining the known quantities.

   Initial cost of pencils: $10

   Charge per pencil: $0.50

2. Identify the slope and the *y*-intercept.

   The slope is a rate. Notice the word "each."

   Slope = 0.50

   The *y*-intercept is a starting value. The store *paid* $10. The starting revenue then is –$10.

   y-intercept = –10

3. Substitute the slope and *y*-intercept into the equation $y = mx + b$, where m is the slope and b is the *y*-intercept.

   $m = 0.50$

   $b = -10$

   $y = 0.50x - 10$

4. Change the slope into a fraction in preparation for graphing.

   $$0.50 = \frac{50}{100} = \frac{1}{2}$$

5. Rewrite the equation using the fraction.

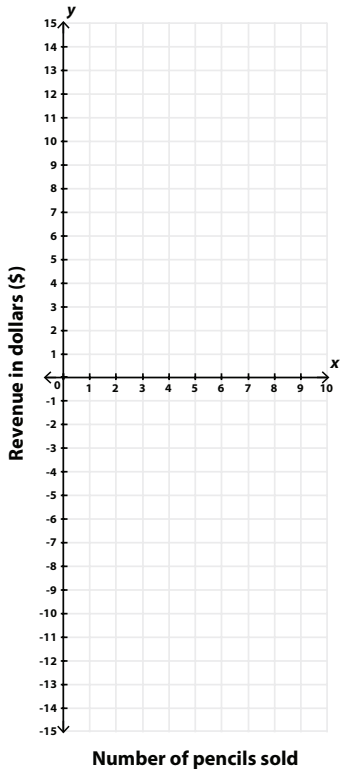
$$y=\frac{1}{2}x-10$$

6. Set up the coordinate plane and identify the independent and dependent variables.

   In this scenario, x represents the number of pencils sold and is the independent variable. The x-axis label is "Number of pencils sold."

   The dependent variable, y, represents the revenue the store will make based on the number of pencils sold. The y-axis label is "Revenue in dollars ($)."

   Determine the scales to be used. Since the slope's rise and run are within 10 units and the y-intercept is –10 units, a scale of 1 on each axis is appropriate. Label the x-axis from 0 to 10 since you will not sell a negative amount of pencils. Label the y-axis from –15 to 15, to allow space to plot the \$10 the store owner paid for the pencils (–10).



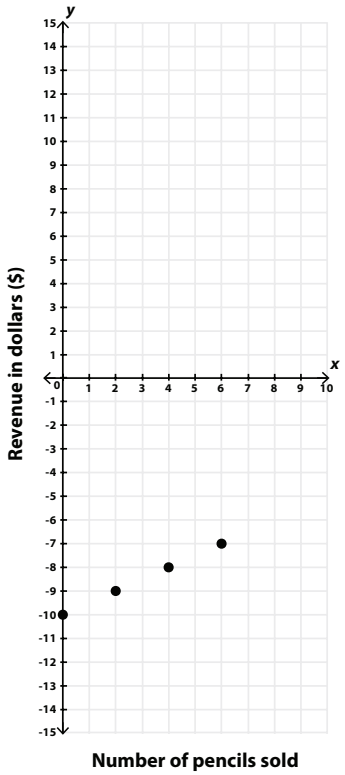
Instruction

7. Plot points using a table of values.

Substitute x values into the equation $y=\frac{1}{2}x-10$ and solve for y.

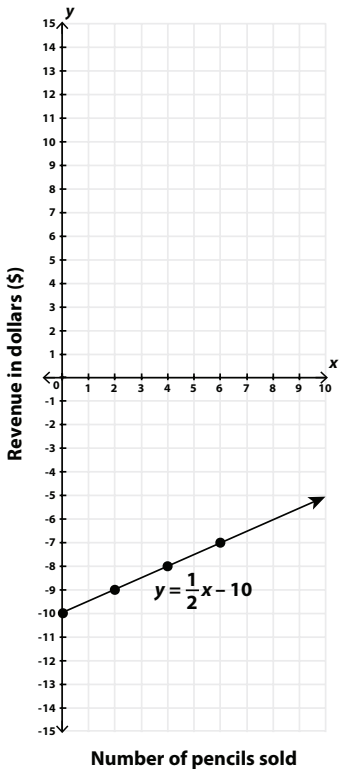
Choose any values of x to substitute. Here, it's easiest to use values of x that are even since after substituting you will be multiplying by $\frac{1}{2}$. Using even-numbered x values will keep the numbers whole after you multiply.

x	y
0	$\frac{1}{2}(0)-10=-10$
2	–9
4	–8
6	–7



Instruction

8. Connect the points with a line and add an arrow at the right end of the line to show that the line of the equation goes on infinitely in that direction. Be sure to write the equation of the line next to the line on the graph.



Instruction

Example 2

A taxi company in Atlanta charges $2.50 per ride plus $2 for every mile driven. Write and graph the equation that models this scenario.

1. Read the problem statement and then reread the problem, determining the known quantities.

   Initial cost of taking a taxi: $2.50

   Charge per mile: $2

2. Identify the slope and the y-intercept.

   The slope is a rate. Notice the word "every."

   Slope = 2

   The y-intercept is a starting value. It costs $2.50 initially to hire a cab driver.

   y-intercept = 2.50

3. Substitute the slope and y-intercept into the equation $y = mx + b$, where m is the slope and b is the y-intercept.

   $m = 2$

   $b = 2.50$

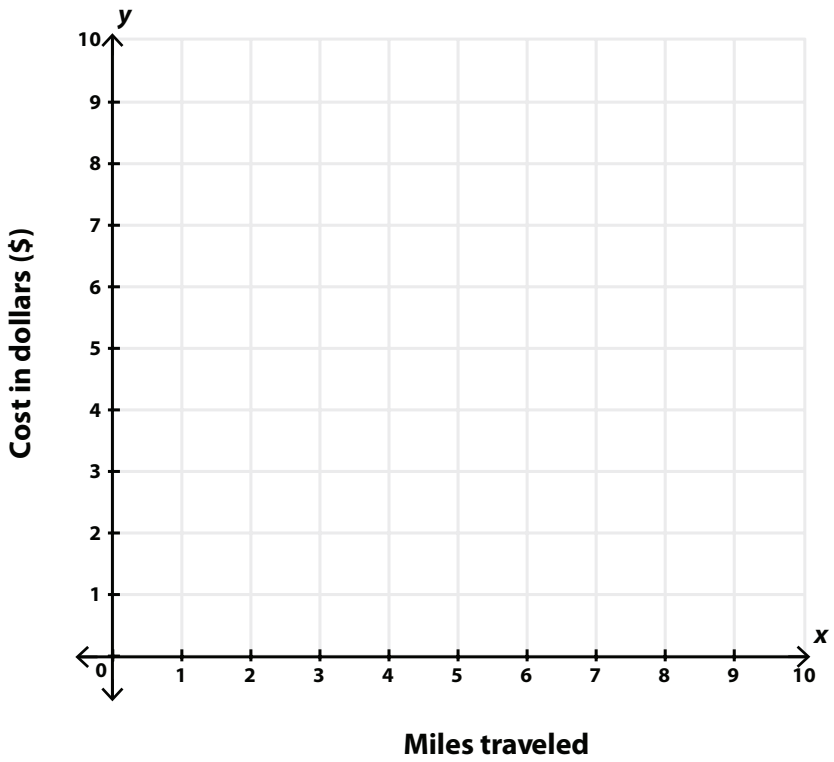
   $y = 2x + 2.50$

4. Set up the coordinate plane.

   In this scenario, x represents the number of miles traveled in the cab and is the independent variable. The x-axis label is "Miles traveled."

   The dependent variable, y, represents the cost of taking a cab based on the number of miles traveled. The y-axis label is "Cost in dollars ($)."

   Determine the scales to be used. Since the slope's rise and run are within 10 units and the y-intercept is within 10 units of 0, a scale of 1 on each axis is appropriate. Label the x-axis from 0 to 10, since miles traveled will only be positive. Label the y-axis from 0 to 10, since cost will only be positive.

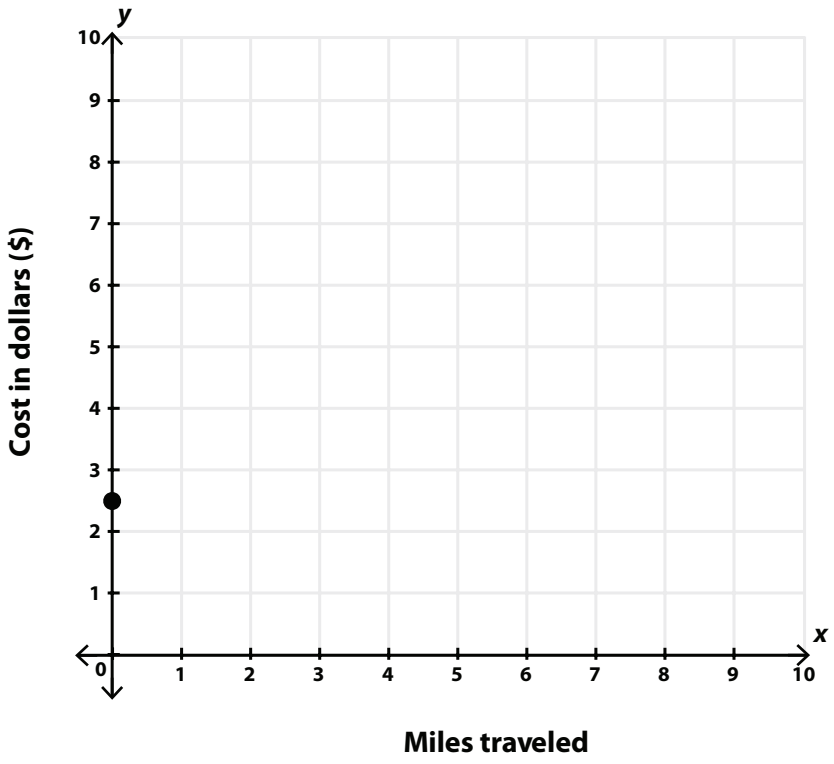


Instruction

5. Graph the equation using the slope and *y*-intercept. Plot the *y*-intercept first.

   The *y*-intercept is 2.5. Remember that the *y*-intercept is where the graph crosses the *y*-axis and the value of *x* is 0. Therefore, the coordinate of the *y*-intercept will always have 0 for *x*. In this case, the coordinate of the *y*-intercept is (0, 2.5).

   To plot points that lie in between grid lines, use estimation. Since 2.5 is halfway between 2 and 3, plot the point halfway between 2 and 3 on the *y*-axis. Estimate the halfway point.



6. Graph the equation using the slope and *y*-intercept. Use the slope to find the second point.

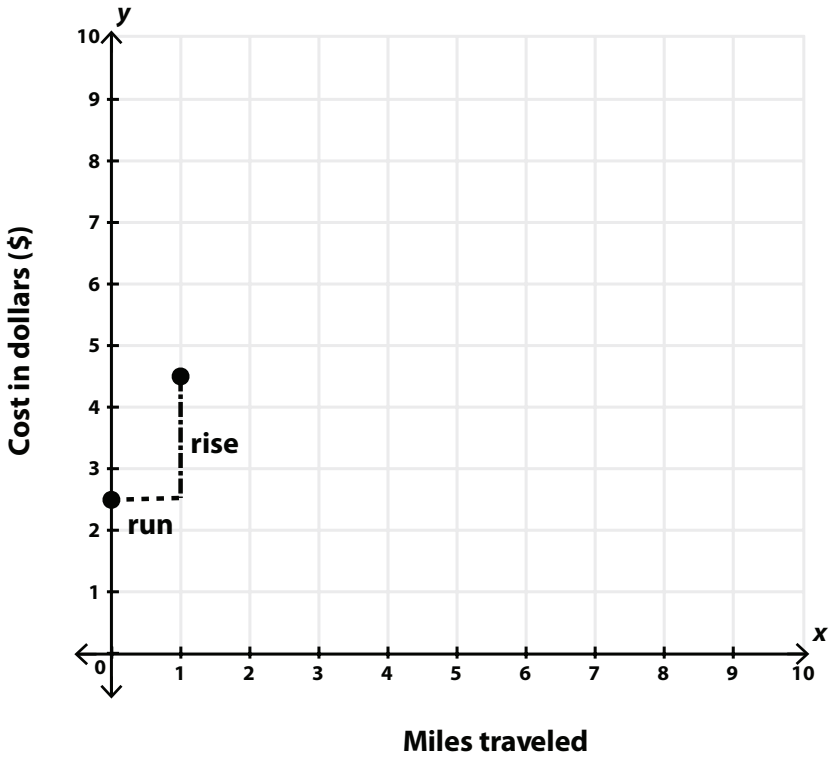
   Remember that the slope is $\frac{\text{rise}}{\text{run}}$. In this case, the slope is 2. Write 2 as a fraction.

   $$2 = \frac{2}{1} = \frac{\text{rise}}{\text{run}}$$

   The rise is 2 and the run is 1.

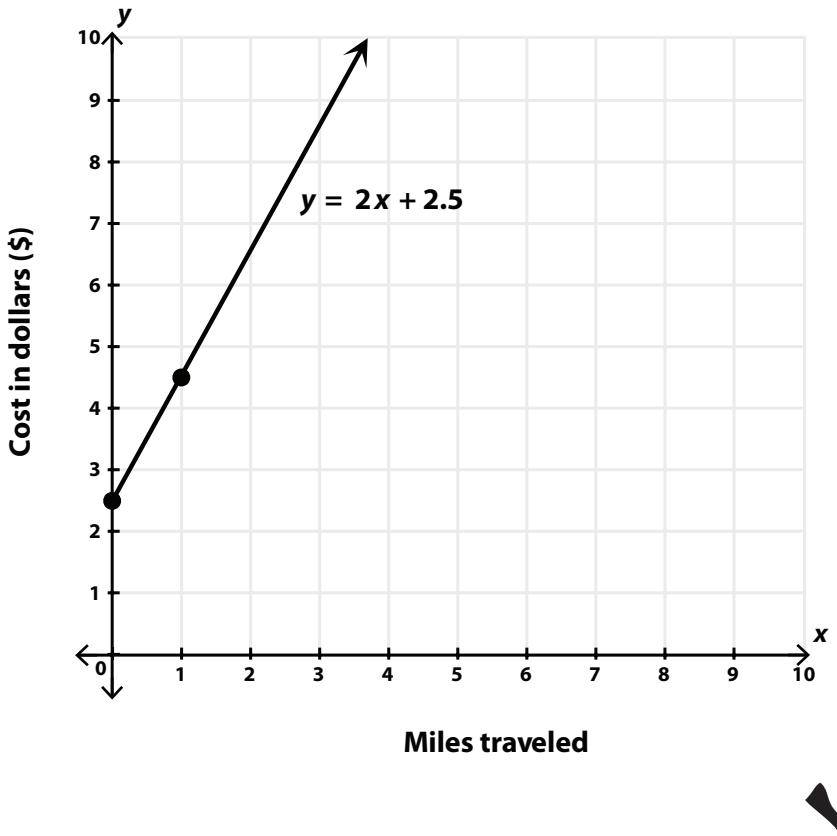
   Point your pencil at the *y*-intercept. Move the pencil up 2 units, since the slope is positive. Remember that the *y*-intercept was halfway between grid lines. Be sure that you move your pencil up 2 complete units by first going to halfway between 3 and 4 (3.5) and then halfway between 4 and 5 (4.5) on the *y*-axis.

   Now, move your pencil to the right 1 unit for the run and plot a point. This is your second point.



7. Connect the points and extend the line. Then, label your line.

   Draw a line through the two points and add an arrow to the right end of the line to show that the line of the equation continues infinitely in that direction. Label the line with the equation, $y = 2x + 2.5$.



Instruction

Example 3

Miranda gets paid $300 a week to deliver groceries. She also earns 5% commission on any orders she collects while out on her delivery run. Write an equation that represents her weekly pay and then graph the equation.

1. Read the problem statement and then reread the problem, determining the known quantities.

   Weekly payment: $300

   Commission: 5% = 0.05

2. Identify the slope and the *y*-intercept.

   The slope is a rate. Notice the symbol "%," which means *percent*, or *per 100*.

   Slope = 0.05

   The *y*-intercept is a starting value. She gets paid $300 a week to start with before taking any orders.

   y-intercept = 300

3. Substitute the slope and *y*-intercept into the equation $y = mx + b$, where m is the slope and b is the *y*-intercept.

   $m = 0.05$

   $b = 300$

   $y = 0.05x + 300$

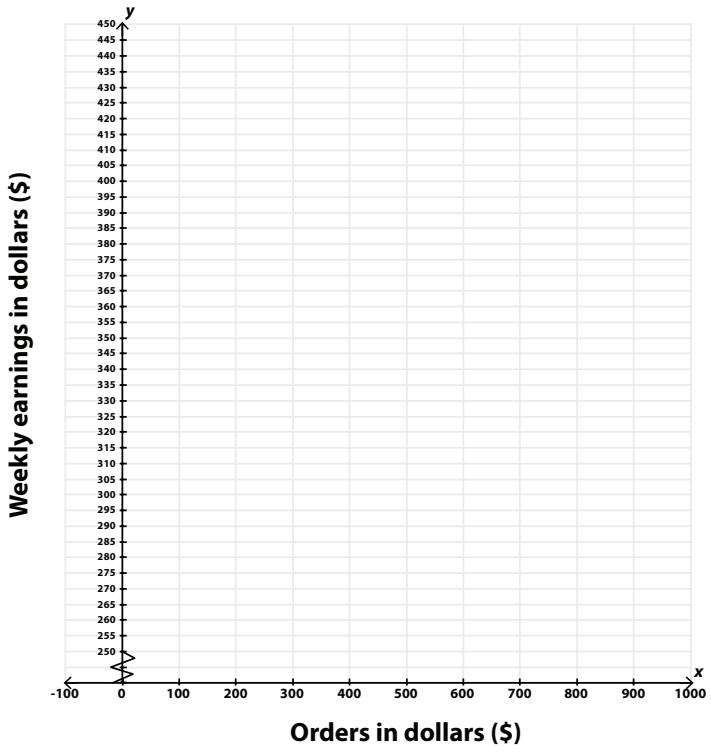
4. Set up the coordinate plane.

   In this scenario, x represents the amount of money in orders Miranda gets. The x-axis label is "Orders in dollars ($)."

   The dependent variable, y, represents her total earnings in a week. The y-axis label is "Weekly earnings in dollars ($)."

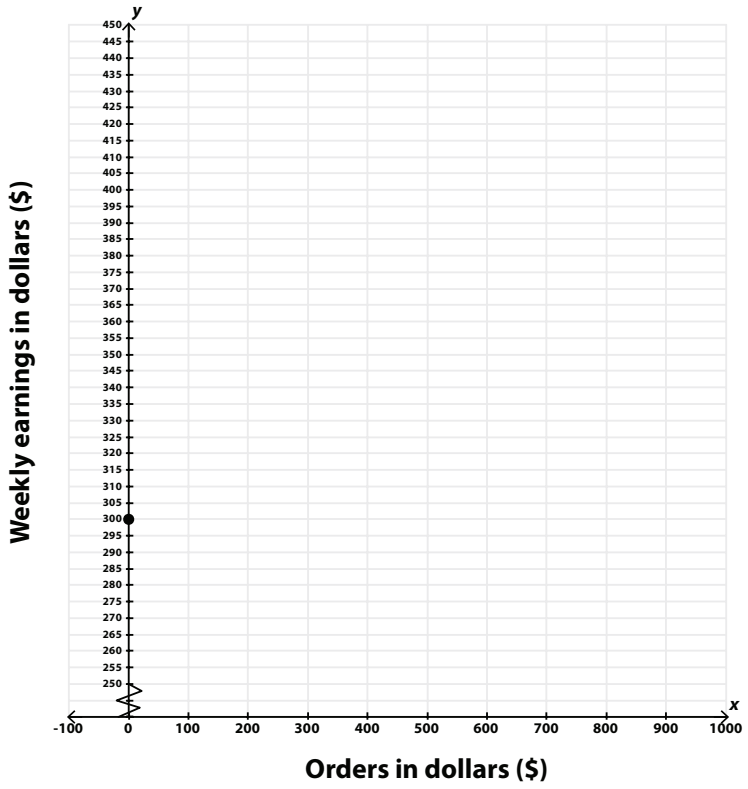
   Determine the scales to be used. The y-intercept is in the hundreds and the slope is in decimals. Work with the slope first. The slope is 0.05 or $\frac{5}{100}$. The rise is a small number, but the run is big. The run is shown on the x-axis, so that will need to be in increments of 100. Start at –100 or 0 since the order amounts will be positive and continue to 1,000.

   The rise is shown on the y-axis and is small, but remember that the y-intercept is $300. Since there's such a large gap before the y-intercept, the y-axis will need to skip values so the graph doesn't become too large. Start the y-axis at 0, then skip to 250 and label the rest of the axis in increments of 5 until you reach 450. Use the zigzag line to show you skipped values between 0 and 250.



5. Graph the equation using the slope and *y*-intercept. Plot the *y*-intercept first.

   The *y*-intercept is 300. Remember that the *y*-intercept is where the graph crosses the *y*-axis and the value of *x* is 0. Therefore, the coordinate of the *y*-intercept will always have 0 for *x*. In this case, the coordinate of the *y*-intercept is (0, 300).



6. Graph the equation using the slope and *y*-intercept. Use the slope to find the second point.

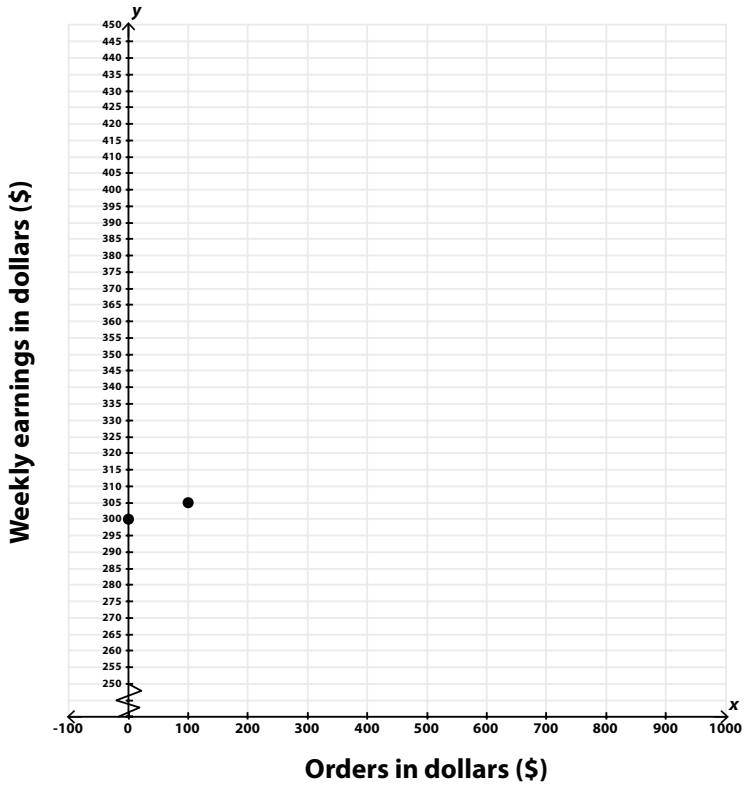
   Remember that the slope is $\frac{\text{rise}}{\text{run}}$. In this case, the slope is 0.05. Rewrite 0.05 as a fraction.

   $$0.05 = \frac{5}{100} = \frac{\text{rise}}{\text{run}}$$

   The rise is 5 and the run is 100.

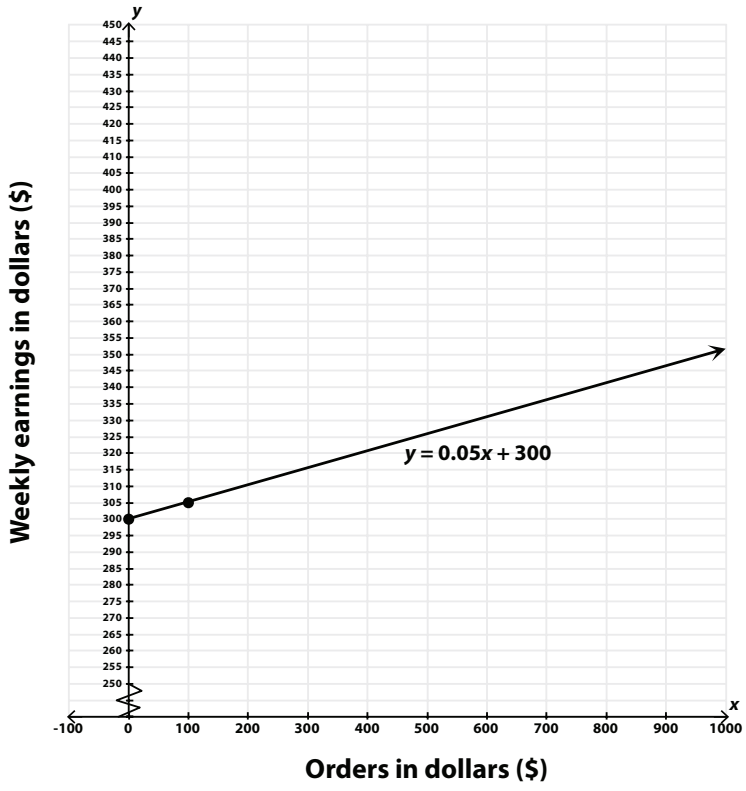
   Place your pencil on the *y*-intercept. Move the pencil up 5 units, since the slope is positive. On this grid, 5 units is one tick mark.

   Now, move your pencil to the right 100 units for the run and plot a point. On this grid, 100 units to the right is one tick mark. This is your second point.



7. Connect the points and extend the line. Then, label your line.

   Draw a line through the two points and add an arrow to the right end of the line to show that the line continues infinitely in that direction. Label your line with the equation, $y = 0.05x + 300$.



Instruction

Example 4

The velocity (or speed) of a ball thrown directly upward can be modeled with the following equation: $v = -gt + v_0$, where v is the speed, g is the force of gravity, t is the elapsed time, and v_0 is the initial velocity at time 0. If the force of gravity is equal to 32 feet per second, and the initial velocity of the ball is 96 feet per second, what is the equation that represents the velocity of the ball? Graph the equation.

1. Read the problem statement and then reread the problem, determining the known quantities.

   Initial velocity: 96 ft/s

   Force of gravity: 32 ft/s

   Notice that in the given equation, the force of gravity is negative. This is due to gravity acting on the ball, pulling it back to Earth and slowing the ball down from its initial velocity.

2. Identify the slope and the y-intercept.

   Notice the form of the given equation for velocity is the same form as $y = mx + b$, where $y = v$, $m = -g$, $x = t$, and $b = v_0$. Therefore, the slope = –32 and the y-intercept = 96.

3. Substitute the slope and y-intercept into the equation $y = mx + b$, where m is the slope and b is the y-intercept.

   $m = -g = -32$

   $b = v_0 = 96$

   $y = -32x + 96$

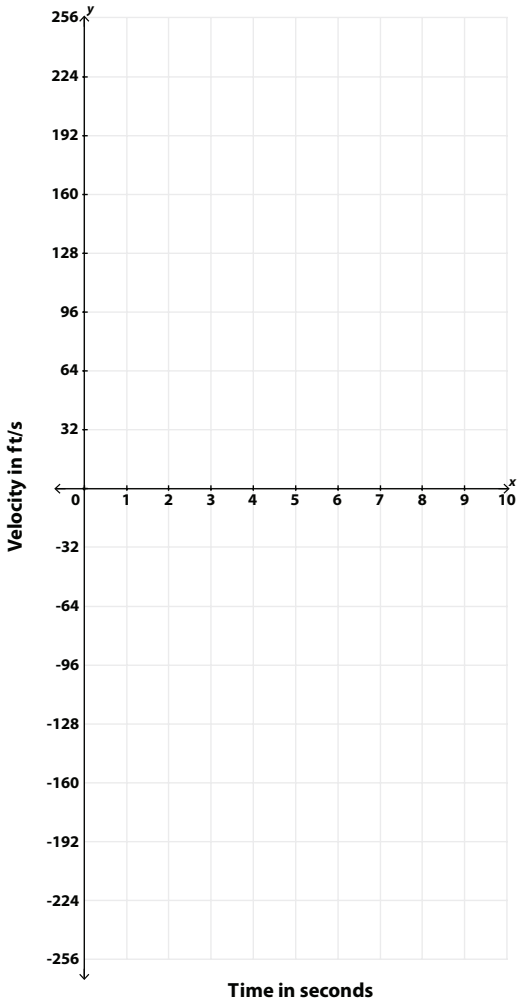
Instruction

4. Set up the coordinate plane.

   In this scenario, x represents the time passing after the ball was dropped. The x-axis label is "Time in seconds."

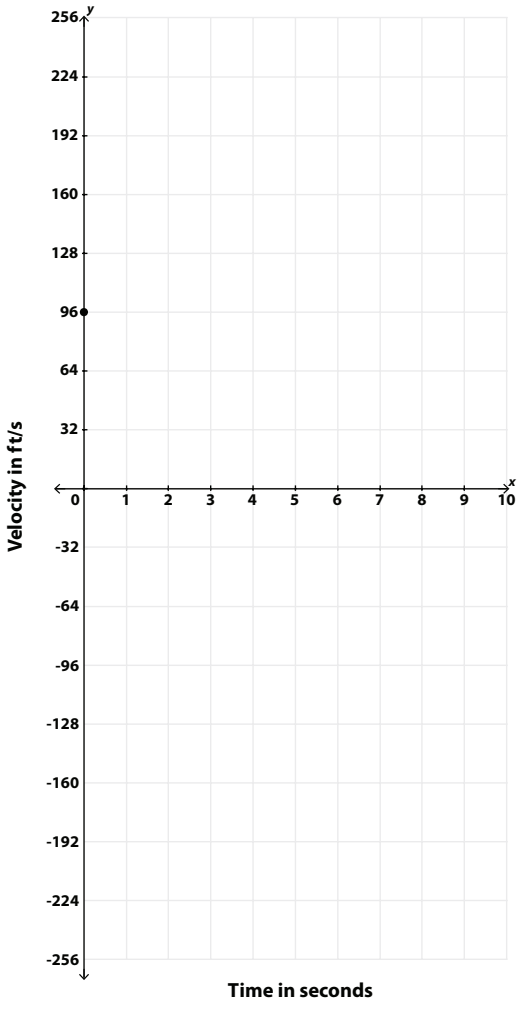
   The dependent variable, y, represents the velocity, or speed, of the ball. The y-axis label is "Velocity in ft/s."

   Determine the scales to be used. The y-intercept is close to 100 and the slope is 32. Notice that 96 (the y-intercept) is a multiple of 32. The y-axis can be labeled in units of 32. Since the x-axis is in seconds, it makes sense that these units are in increments of 1. Since time cannot be negative, use only a positive scale for the x-axis.



5. Graph the equation using the slope and *y*-intercept. Plot the *y*-intercept first.

   The *y*-intercept is 96. Remember that the *y*-intercept is where the graph crosses the *y*-axis and the value of *x* is 0. Therefore, the coordinate of the *y*-intercept will always have 0 for *x*. In this case, the coordinate of the *y*-intercept is (0, 96).



6. Graph the equation using the slope and *y*-intercept. Use the slope to find the second point.

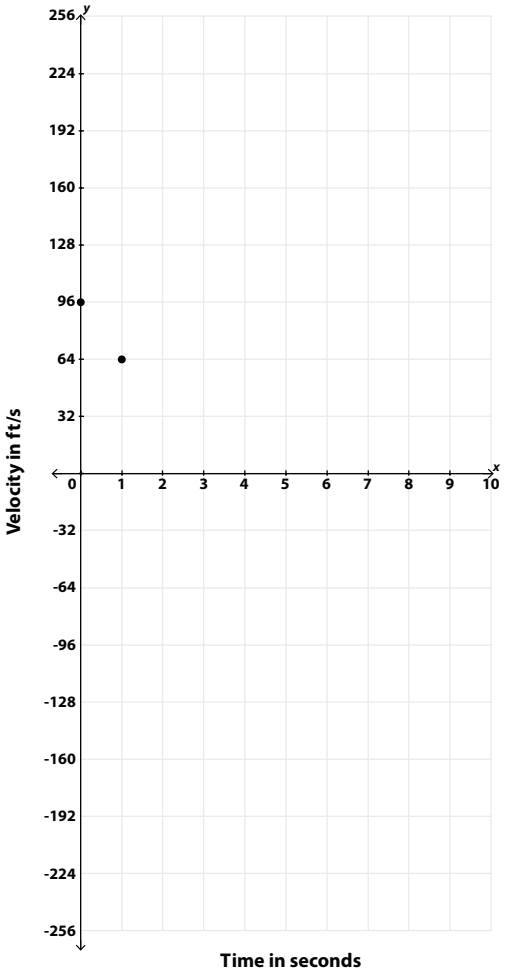
   Remember that the slope is $\frac{\text{rise}}{\text{run}}$. In this case, the slope is –32. Rewrite –32 as a fraction.

   $$-32 = \frac{-32}{1} = \frac{\text{rise}}{\text{run}}$$

   The rise is –32 and the run is 1.

   Place your pencil on the *y*-intercept. Move the pencil down 32 units, since the slope is negative. On this grid, 32 units is one tick mark.

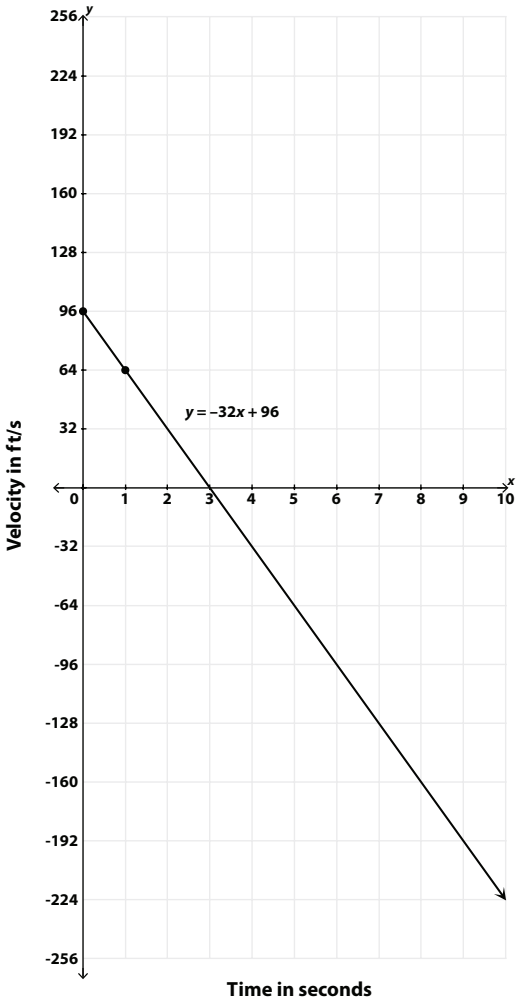
   Now, move your pencil to the right 1 unit for the run and plot a point. This is your second point.



Instruction

7. Connect the points and extend the line toward the right. Then, label your line.

   Draw a line through the two points and add an arrow to the right end of the line to show that the line of the equation continues infinitely in that direction. Label your line with the equation $y = -32x + 96$.



Instruction

Example 5

A Boeing 747 starts out a long flight with about 57,260 gallons of fuel in its tank. The airplane uses an average of 5 gallons of fuel per mile. Write an equation that models the amount of fuel in the tank and then graph the equation using a graphing calculator.

1. Read the problem statement and then reread the problem, determining the known quantities.

   Starting fuel tank amount: 57,260 gallons

   Rate of fuel consumption: 5 gallons per mile

2. Identify the slope and the y-intercept.

   The slope is a rate. Notice the word "per" in the phrase "5 gallons of fuel per mile." Since the total number of gallons left in the fuel tank is decreasing at this rate, the slope is negative.

   Slope = –5

   The y-intercept is a starting value. The airplane starts out with 57,260 gallons of fuel.

   y-intercept = 57,260

   Substitute the slope and y-intercept into the equation $y = mx + b$, where m is the slope and b is the y-intercept.

   $m = 5$

   $b = 57{,}260$

   $y = -5x + 57{,}260$

Instruction

3. Graph the equation on your calculator.

On a TI-83/84:

Step 1: Press [Y=].

Step 2: At Y_1, type in [(–)][5][X, T, θ, *n*][+][57260].

Step 3: Press [WINDOW] to change the viewing window.

Step 4: At Xmin, enter [0] and arrow down 1 level to Xmax.

Step 5: At Xmax, enter [3000] and arrow down 1 level to Xscl.

Step 6: At Xscl, enter [100] and arrow down 1 level to Ymin.

Step 7: At Ymin, enter [40000] and arrow down 1 level to Ymax.

Step 8: At Ymax, enter [58000] and arrow down 1 level to Yscl.

Step 9: At Yscl, enter [1000].

Step 10: Press [GRAPH].

On a TI-Nspire:

Step 1: Press the [home] key.

Step 2: Arrow over to the graphing icon and press [enter].

Step 3: At the blinking cursor at the bottom of the screen, enter in the equation [(–)][5][x][+][57260] and press [enter].

Step 4: Change the viewing window by pressing [menu], arrowing down to number 4: Window/Zoom, and clicking the center button of the navigation pad.

Step 5: Choose 1: Window settings by pressing the center button.

Step 6: Enter in the appropriate XMin value, [0], then press [tab].

Step 7: Enter in the appropriate XMax value, [3000], then press [tab].

Step 8: Leave the XScale set to "Auto." Press [tab] twice to navigate to YMin and enter [40000].

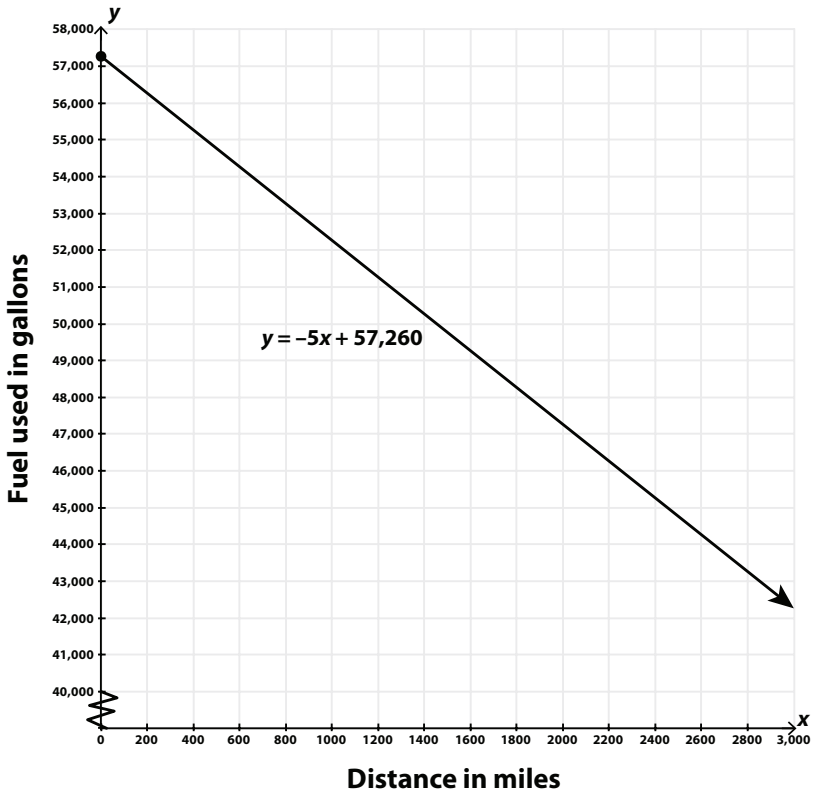
Step 9: Press [tab] to navigate to YMax. Enter [58000]. Press [tab] twice to leave YScale set to "auto" and to navigate to "OK."

Step 10: Press [enter].

Step 11: Press [menu] and select 2: View and 5: Show Grid.

4. Redraw the graph on graph paper.

   On the TI-83/84, the scale was entered in [WINDOW] settings. The X scale was 100 and the Y scale was 1,000. Set up the graph paper using these scales. Label the *y*-axis "Fuel used in gallons." Show a break in the graph from 0 to 40,000 using a zigzag line. Label the *x*-axis "Distance in miles." To show the table on the calculator so you can plot points, press [2nd][GRAPH]. The table shows two columns with values; the first column holds the *x*-values, and the second column holds the *y*-values. Pick a pair to plot, and then connect the line. To return to the graph, press [GRAPH]. Remember to label the line with the equation. (*Note:* It may take you a few tries to get the window settings the way you want. The graph that follows shows an X scale of 200 so that you can easily see the full extent of the graphed line.)



(*continued*)

Instruction

If you used a TI-Nspire, determine the scale that was used by counting the dots on the grid from your minimum *y*-value to your maximum *y*-value. In this case, there are 18 dots vertically between 40,000 and 58,000. The difference between the YMax and YMin values is 18,000. Divide that by the number of dots (18). The result (1,000) is the scale.

$$\frac{\text{Y Max} - \text{Y Min}}{\text{Number of dots}} = \frac{58{,}000 - 40{,}000}{18} = \frac{18{,}000}{18} = 1000$$

This means each dot is worth 1,000 units vertically. Label the *y*-axis "Fuel used in gallons." Use a zigzag line to show a break in the graph from 0 to 40,000.

Repeat the same process for determining the *x*-axis scale. The XMin = 0 and XMax = 3000. The number of dots = 30.

$$\frac{\text{X Max} - \text{X Min}}{\text{Number of dots}} = \frac{3000 - 0}{30} = \frac{3000}{30} = 100$$

This means each dot is worth 100 units horizontally.

Set up your graph paper accordingly. Label the *x*-axis "Distance in miles."

On your calculator, you need to show the table in order to plot points. To show the table, press [tab][T]. To navigate within the table, use the navigation pad. The table shows two columns with values; the first column holds the *x*-values, and the second column holds the *y*-values. Pick a pair to plot and then connect the line. Remember to label the line with the equation. To hide the table, navigate back to the graph by pressing [ctrl][tab]. Then press [ctrl][T].