

**LESSON****12-4****Problem Solving*****Point-Slope Form***

**Write the correct answer.**

1. A 1600 square foot home in Houston will sell for about \$102,000. The price increases about \$43.41 per square foot. Write an equation that describes the price  $y$  of a house in Houston, based on the square footage  $x$ .  
\_\_\_\_\_
2. Write the equation in Exercise 1 in slope-intercept form.  
\_\_\_\_\_
3. Wind chill is a measure of what temperature feels like with the wind. With a 25 mph wind, 40°F will feel like 29°F. Write an equation in point-slope form that describes the wind chill  $y$  based on the temperature  $x$ , if the slope of the line is 1.337.  
\_\_\_\_\_
4. With a 25 mph wind, what does a temperature of 0°F feel like?  
\_\_\_\_\_

**From 2 to 13 years, the growth rate for children is generally linear. Choose the letter of the correct answer.**

5. The average height of a 2-year old boy is 36 inches, and the average growth rate per year is 2.2 inches. Write an equation in point-slope form that describes the height of a boy  $y$  based on his age  $x$ .  
**A**  $y - 36 = 2(x - 2.2)$   
**B**  $y - 2 = 2.2(x - 36)$   
**C**  $y - 36 = 2.2(x - 2)$   
**D**  $y - 2.2 = 2(x - 36)$
6. The average height of a 5-year old girl is 44 inches, and the average growth rate per year is 2.4 inches. Write an equation in point-slope form that describes the height of a girl  $y$  based on her age  $x$ .  
**F**  $y - 2.4 = 44(x - 5)$   
**G**  $y - 44 = 2.4(x - 5)$   
**H**  $y - 44 = 5(x - 2.4)$   
**J**  $y - 5 = 2.4(x - 44)$
7. Write the equation from Exercise 6 in slope-intercept form.  
**A**  $y = 2.4x - 100.6$   
**B**  $y = 44x - 217.6$   
**C**  $y = 5x + 32$   
**D**  $y = 2.4x + 32$
8. Use the equation in Exercise 6 to find the average height of a 13-year old girl.  
**F** 56.3 in.  
**G** 63.2 in.  
**H** 69.4 in.  
**J** 97 in.

## LESSON 12-4 Problem Solving

### 12-4 Point-Slope Form

Write the correct answer.

1. A 1600 square foot home in Houston will sell for about \$102,000. The price increases about \$43.41 per square foot. Write an equation that describes the price  $y$  of a house in Houston, based on the square footage  $x$ .

$$y - 102,000 = 43.41(x - 1600)$$

3. Wind chill is a measure of what temperature feels like with the wind. With a 25 mph wind,  $40^\circ\text{F}$  will feel like  $29^\circ\text{F}$ . Write an equation in point-slope form that describes the wind chill  $y$  based on the temperature  $x$ , if the slope of the line is 1.337.

$$y - 29 = 1.337(x - 40)$$

2. Write the equation in Exercise 1 in slope-intercept form.

$$y = 43.41x + 32,544$$

4. With a 25 mph wind, what does a temperature of  $0^\circ\text{F}$  feel like?

$$-24.48^\circ\text{F}$$

From 2 to 13 years, the growth rate for children is generally linear. Choose the letter of the correct answer.

5. The average height of a 2-year old boy is 36 inches, and the average growth rate per year is 2.2 inches. Write an equation in point-slope form that describes the height of a boy  $y$  based on his age  $x$ .

- A  $y - 36 = 2(x - 2.2)$   
B  $y - 2 = 2.2(x - 36)$   
C  $y - 36 = 2.2(x - 2)$   
D  $y - 2.2 = 2(x - 36)$

6. The average height of a 5-year old girl is 44 inches, and the average growth rate per year is 2.4 inches. Write an equation in point-slope form that describes the height of a girl  $y$  based on her age  $x$ .

- F  $y - 2.4 = 44(x - 5)$   
G  $y - 44 = 2.4(x - 5)$   
H  $y - 44 = 5(x - 2.4)$   
J  $y - 5 = 2.4(x - 44)$

7. Write the equation from Exercise 6 in slope-intercept form.

- A  $y = 2.4x - 100.6$   
B  $y = 44x - 217.6$   
C  $y = 5x + 32$   
D  $y = 2.4x + 32$

8. Use the equation in Exercise 6 to find the average height of a 13-year old girl.

- F 56.3 in.  
G 63.2 in.  
H 69.4 in.  
J 97 in.

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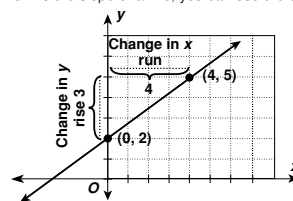
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## LESSON 12-4 Reading Strategies

### 12-4 Use a Procedure

To find the slope of a line, you can use the coordinates for two points on the line.



**Step 1:** Subtract to find the difference between the  $y$ -coordinates of the two points:  $5 - 2 = 3$ .

**Step 2:** Subtract to find the difference between the  $x$ -coordinates of the two points:  $4 - 0 = 4$ .

**Step 3:** Write the ratio of the differences. The difference between the  $y$ -coordinates is 3. The difference between the  $x$ -coordinates is 4. The slope is the ratio  $\frac{3}{4}$ .

When you have the slope of a line and a point it passes through, you can write an equation for the line in **point-slope form**.

Point on the line	Slope	Point-slope form
$(x_1, y_1)$	$m$	$y - y_1 = m(x - x_1)$
$(4, 5)$	$\frac{3}{4}$	$y - 5 = \frac{3}{4}(x - 4)$

Use the above example to answer each question.

1. What ratio is shown by the slope of a line?

change in  $y$  or rise  
change in  $x$ , or run

2. How can you find the slope of a line?

Possible answer: Find the difference between the  $y$ -values of two points and find the difference between the  $x$ -values of the same points; write the differences as a ratio.

3. What information do you need to write an equation for a line in point-slope form?

coordinates of a point the line passes through and slope of the line

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## LESSON 12-4 Puzzles, Twisters & Teasers

### 12-4 Get a Clue!

Identify a point on each line and the slope of the line. Then use the slope values to answer the riddle.

- |                                   |                                    |  |          |
|-----------------------------------|------------------------------------|--|----------|
| 1. $y + 1 = \frac{2}{3}(x + 7)$   | point = <u><math>-7, -1</math></u> | slope = <u><math>\frac{2}{3}</math></u>  | <b>S</b> |
| 2. $y + 1 = 11(x - 1)$            | point = <u><math>1, -1</math></u>  | slope = <u><math>11</math></u>           | <b>C</b> |
| 3. $y - 2 = -\frac{1}{6}(x - 11)$ | point = <u><math>11, 2</math></u>  | slope = <u><math>-\frac{1}{6}</math></u> | <b>N</b> |
| 4. $y + 7 = 1(x - 5)$             | point = <u><math>5, -7</math></u>  | slope = <u><math>1</math></u>            | <b>L</b> |
| 5. $y + 7 = 3(x + 4)$             | point = <u><math>-4, -7</math></u> | slope = <u><math>3</math></u>            | <b>E</b> |
| 6. $y - 9 = 5(x - 12)$            | point = <u><math>12, 9</math></u>  | slope = <u><math>5</math></u>            | <b>B</b> |
| 7. $y - 11 = 14(x - 8)$           | point = <u><math>8, 11</math></u>  | slope = <u><math>14</math></u>           | <b>H</b> |
| 8. $y - 4 = -2(x + 7)$            | point = <u><math>-7, 4</math></u>  | slope = <u><math>-2</math></u>           | <b>O</b> |
| 9. $y - 3 = -1.8(x - 5.6)$        | point = <u><math>5.6, 3</math></u> | slope = <u><math>-1.8</math></u>         | <b>R</b> |
| 10. $y + 8 = -6(x - 9)$           | point = <u><math>9, -8</math></u>  | slope = <u><math>-6</math></u>           | <b>K</b> |

What do you call a dog detective?

S	H	E	R	L	O	C	K
$\frac{2}{3}$	14	3	-1.8	1	-2	11	-6
B	O	N	E	S			
5	-2	$-\frac{1}{6}$	3	$\frac{2}{3}$			



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## LESSON 12-5 Practice A

### 12-5 Direct Variation

The following tables show direct variation for the given equation. Complete the missing information in the tables.

1.  $y = 2x$

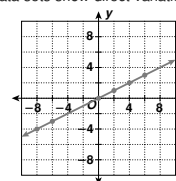
$x$	-10	-7	-4	3	6	12	15	22
$y$	-20	-14	-8	6	12	24	30	44

2.  $y = \frac{1}{3}x$

$x$	-21	-15	-9	3	8	12	19	30
$y$	-7	-5	-3	1	$2\frac{2}{3}$	4	$6\frac{1}{3}$	10

3. Make a graph to determine whether the data sets show direct variation.

$x$	-8	-6	0	2	4	6
$y$	-4	-3	0	1	2	3



The data sets show direct variation.

Find each equation of direct variation, given that  $y$  varies directly with  $x$ .

4.  $y$  is 10 when  $x$  is 2.

$$y = 5x$$

5.  $y$  is 42 when  $x$  is -6.

$$y = -7x$$

6.  $y$  is -50 when  $x$  is 5.

$$y = -10x$$

7.  $y$  is 15 when  $x$  is 30.

$$y = \frac{1}{2}x$$

8. At a constant speed, the gasoline a car uses varies directly with the distance the car travels. A car uses 10 gallons of gasoline to travel 210 miles. How many gallons will the car use to travel 294 miles?

14 gallons

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